Structured Electronic Design
All-pole loop gain and servo bandwidth

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Denominator coefficient of highest order of s determined by loop gain-poles (LP) product

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Denominator coefficient of highest order of s determined by loop gain-poles (LP) product

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loop gain-poles (LP) product

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